

Problem Statement:

1. Construct an optimal on-line scheduling algorithm:

If the task set is schedulable with the energy generated by a given energy source, an optimal algorithm determines a feasible schedule.

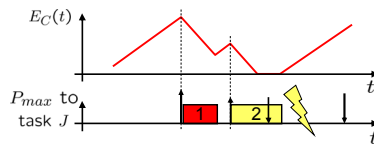
2. Construct an admittance test :

Determine, whether a set of event streams with a given characteristic is schedulable given a certain energy source.

Naive approaches fail

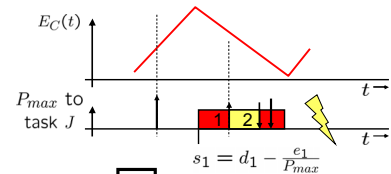
Scenario I: scheduling with Earliest Deadline First (EDF) algorithm

Result: Greedy scheduling is not suited.



Scenario II: scheduling based on As-Late-As-Possible (ALAP) principle

Result: ALAP does not work either.



Result 1: Optimal Lazy Scheduling Algorithm (LSA)

optimal starting time s_i

$$s_i = d_i - \frac{\min(E_C(a_i) + E_S(a_i, d_i), C + E_S(s_i, d_i))}{P_{max}}$$

Rule 1: All tasks with $s_i \leq t$ are processed with EDF scheduling using P_{max} .

Rule 2: If there is no task with $s_i \leq t$ and the energy storage is full, all incoming power $P_S(t)$ is assigned to the task with the currently earliest deadline.

Theorem 1 (Optimality of LSA)

Assume a system (C, P_{max}) is driven by an energy source E_S . If LSA cannot schedule a given task set, then no other scheduling algorithm is able to schedule it.

Note:

Lazy Scheduling algorithms are energy-clairvoyant, i.e. the energy $E_S(a_i, d_i)$ has to be known in advance to calculate s_i . Therefore, a practical algorithm has to predict the future energy $E_S(a_i, d_i)$.

Event stream model:

- delay requirement d
- energy request per event e
- maximum number $\alpha(\Delta)$ of events observed in any interval Δ

Energy Source Model:

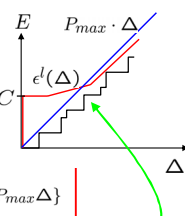
- minimum energy $e^l(\Delta)$ generated in any interval Δ

Result 2: Admittance Test

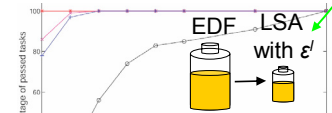
Theorem 2 (Admittance Test):

A given set of event streams $J_i, i \in I$ is schedulable with initially stored energy $E_C(0) = C$, iff

$$\forall \Delta : \sum_{i \in I} e_i \alpha_i(\Delta - d_i) \leq \min\{e^l(\Delta) + C, P_{max} \Delta\}$$



Simulation Results:



Comparison: LSA using e^l as energy predictor versus EDF

Result: capacity savings of ~40% for random task sets for LSA

References:

- C.Moser, D.Brunelli, L.Thiele, L.Benini: Real-Time Scheduling for Energy Harvesting Sensor Nodes. Int. Journal Real-Time Systems, January 2007.
- C.Moser, D.Brunelli, L.Thiele, L.Benini: Lazy Scheduling for Energy Harvesting Sensor Nodes. 5th IFIP Conf. on Distr. and Parallel Embedded Systems DIPES, Portugal, October 2006.
- C.Moser, D.Brunelli, L.Thiele, L.Benini: Real-Time Scheduling with Regenerative Energy. 18th Euromicro Conference on Real-Time Systems ECRTS, Germany, July 2006.